

Interactions with Matter

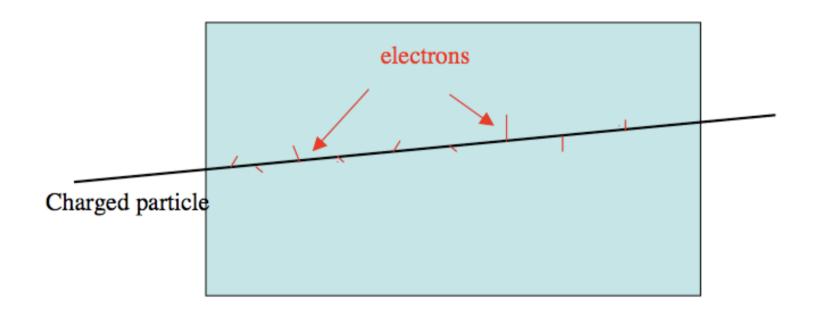
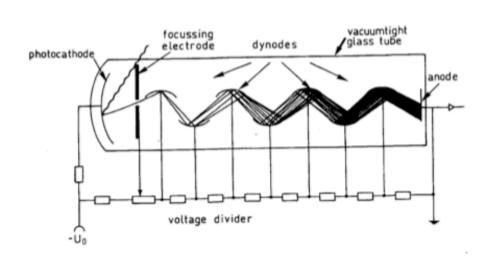
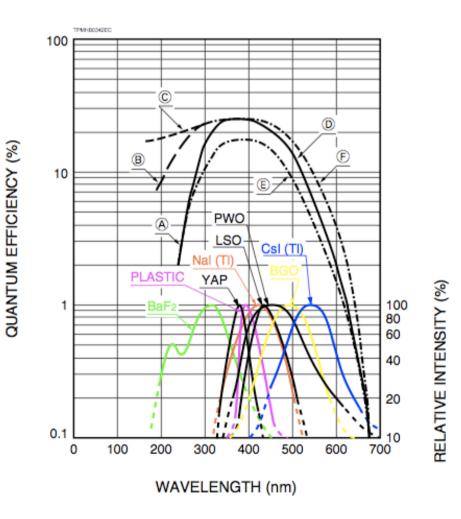


Photo-multipliers

Photomultipliers



Conversion via photoelectric effect: One photon to one electron, electrons multiplied Typical efficiencies: up to 25%



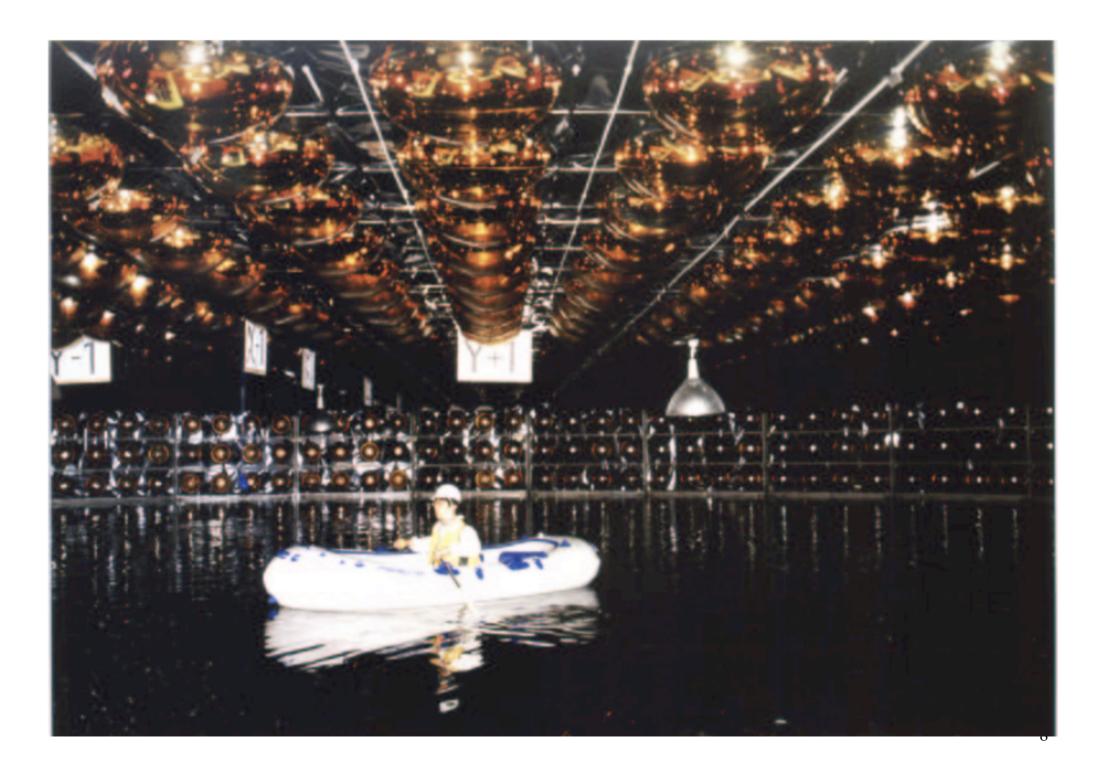
Photomultipliers





Available from 3/8 inch diameters to ≈ 40 cm diameter. Entrance windows on top ("head on") or on sides ("side on")



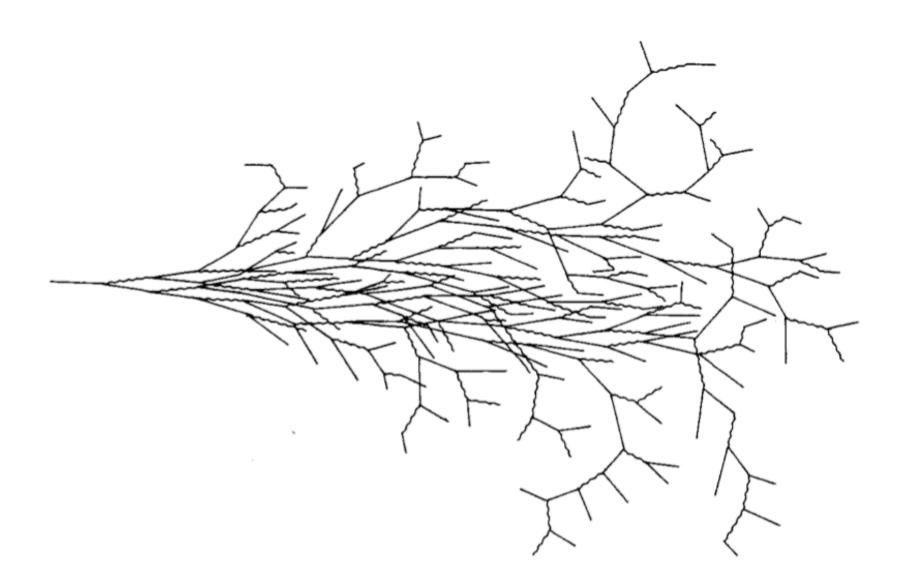


Calorimeters

Calorimeters: Why?

- Measure *charged* + *neutral* particles
- Obtain information on energy flow:
 Total (missing) transverse energy, jets, etc.
- Obtain information fast
 recognize and select interesting events in real time (trigger)
- Performance of calorimeters *improves with energy* ($\sim E^{-1/2}$ if statistical processes are the limiting factor)

A Shower...



Calorimeters

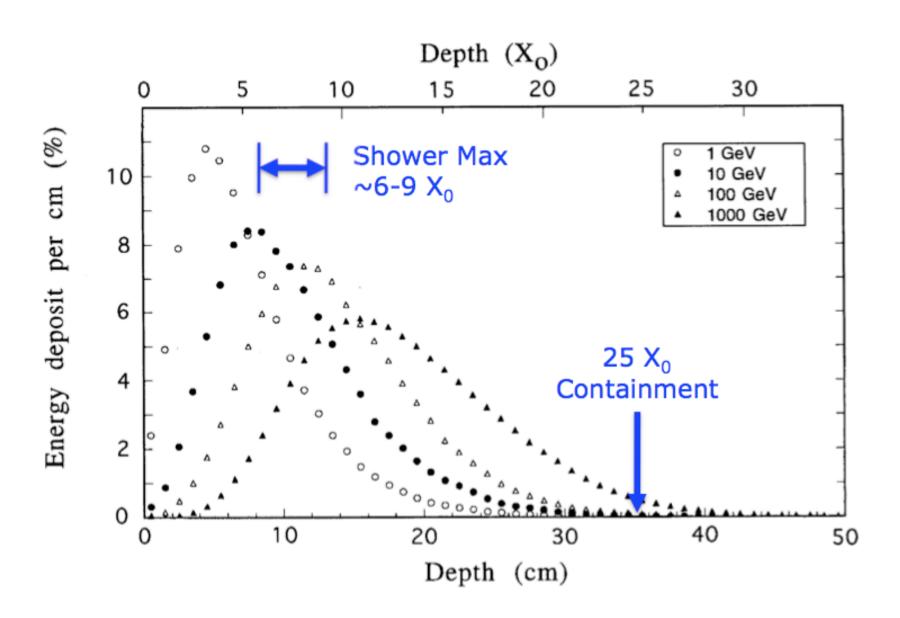
Shower has to be absorbed totally. If not: reduced resolution due to fluctuations

different optimization needed for electrons/photons and hadrons

- for electrons/photons: governed by Radiation Length X_0
- for hadrons: governed by Interaction Length λ_I

for hadrons in addition: Need "compensation" due to electromagnetic part of shower.

Electromagnetic Showers



Electromagnetic Showers

Photon → Pair Production Electron / positron → Bremsstrahlung (Photon)

• Simple Model, measured in "steps" t (one conversion, related to Radiation length X_0):

Number of Particles: $N(t) = 2^t$

Energy of particles: $E(t) = E_0 \cdot 2^{-t}$

Multiplication stops if $E(t) < E_c$ $E_c = E_0 \cdot 2^{-t_{\text{max}}}$ $E_c :\approx \text{Pair production threshold}$

$$t_{\rm max} = \frac{\ln E_0/E_c}{\ln 2} \propto \ln E_0$$
 position of shower maximum

Total number of shower particles:

$$S = \sum_{t=0}^{t_{ ext{max}}} N(t) = \sum 2^t = 2^{t_{ ext{max}}+1} - 1 pprox 2 \cdot 2^{t_{ ext{max}}} = 2 \cdot rac{E_0}{E_e} \propto E_0$$

Electromagnetic Showers

Total track length (sampling step t, measures in units of X_0)

Project: EM Calorimeters

$$S^{\star} = \frac{S}{t} = 2 \cdot \frac{E_0}{E_c} \cdot \frac{1}{t}$$

Realistic description of longitudinal shower development:

$$\frac{dE}{dt} = \text{const} \cdot t^a \cdot e^{-bt}$$
 (a, b - fit parameter)

Lateral spread, caused by multiple scattering:

Molière Radius
$$R_m = \frac{21 \,\mathrm{MeV}}{E_c} X_0 [\mathrm{g/cm}^2]$$

95 % of shower energy is contained in a cylinder of radius 2 R_m

for homogeneous calorimeters:
$$R_m = \begin{cases} \text{Fe: } 14 \, \text{g/cm}^2 \triangleq 1.8 \, \text{cm} \\ \text{Pb: } 18 \, \text{g/cm}^2 \triangleq 1.6 \, \text{cm} \end{cases}$$

Shower Profile and Containement

- At the shower maximum, the average amplification rate in the shower goes to unity, and we have:
 - Average Particle Energy at Shower Max:

$$E_c$$
 (Pb = 7.4 MeV, Fe = 22 MeV)

Number of Particles at Shower Max:

$$N_{max} = E_0/E_c \propto E_0$$

Total "Path Length" of Showering Particles:

$$L_{tot} \sim N_{max}X_0/ln2 \propto E_0$$

Depth of Shower Max:

$$L_{max} \sim In(E_0/E_c) X_0 \sim 6-9 X_0$$

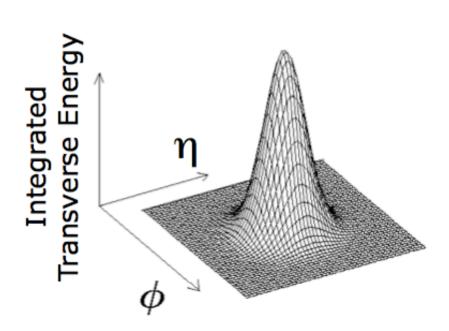
Clearly, from above, if one sampled the total path length or a known fraction of the total path length (every X₀), then there is direct proportionality between the sampled energy and the incident particle energy E₀

14

Electromagnetic Shower

The Characteristic Transverse Size of the EM Shower is given by the Moliere Radius

 $\rho_{\rm M}$ = (21 MeV/E_c) X₀ (99% of shower in $3\rho_{\rm M}$)



Choose Cell Granularity a bit 16 Smaller than One Moliere Radius

FNAL-CERN Summer School 2009 Calorimetry Lecture 1

Energy Resolution

 $\frac{\sigma_E}{E} = \frac{N}{E} \oplus \frac{S}{\sqrt{E}} \oplus C$

- "N" is the electronic noise term and is set by the square root of the number of detector cells being summed (for incoherent noise) and the RMS electronic noise per channel in units of energy, i.e. ~6000e⁻ of preamp electronic noise is to be compared with the number of photoelectrons times the photodetector gain collected per MeV of deposited energy
 S can be 2%-15%
- "S" is the stochastic term and is a form of 1/√N counting statistics (signal quanta counting within a fixed volume)
- "C" is the constant term and comes from intrinsic nonuniformities in how one computes the incident particle energy, i.e. variations in the mean response that depend on parameters that are not tracked (temperature, etc.) 39

Project: derive the resolution formula in calorimeters

Shower Position

- Two common methods for computing the position of a shower within a fraction of the cell size
 - Correction to the center-of-gravity:

$$x_{cog} = \sum_{i} x_{i} E_{i} / \sum_{i} E_{i}$$
$$x_{corr} = A \tan^{-1} (B x_{cog})$$

Logarithmic Weighting:

chmic Weighting:

$$x = \sum_{i} x_{i} w_{i} / \sum_{i} w_{i}$$

$$w_{i} = w_{0} + \ln \left(\frac{E_{i}}{\sum_{i} E_{i}} \right)$$

At energies of ~45 GeV, an electron impacting on a 20mm crystal can have its impact point determined to better than 1mm in both coordinates

Interaction Lenght

- For the pion component, however, the behavior is a bit more clear (though erratic)
 - Pions are in a (nuclear) isospin triplet and therefore "tumble in isospin" with every nucleon they hit – once a charged pion tumbles into a neutral pion, the neutron pion rapidly decays to two photons and initiates an electromagnetic shower "one-way street"

Similarly, $\pi^+/\pi^0/\pi^-$ are produced in equal amounts on average $\lambda_{\rm int} = \lambda_{\rm int} + \lambda_{\rm int}$

Hadronic Showers

Longitudinal development: governed by nuclear interaction length λ_I Lateral development: transverse momentum p_T of particles since $\lambda_I > X_0$ and $\langle p_T \rangle \gg \langle p_T \rangle^{\text{mult. scatt.}}$

⇒ hadron showers are wider and longer than electromagnetic showers

```
Hadron Energy \Rightarrow \begin{cases} \text{charged particles } (\mu \text{'s are lost}) \\ \text{electromagnetic showers via } \pi^0 (e, \gamma; \text{ contained}) \\ \text{nuclear binding energy (can be partially recovered)} \\ \text{nuclear fragments (partially lost)} \end{cases}
```

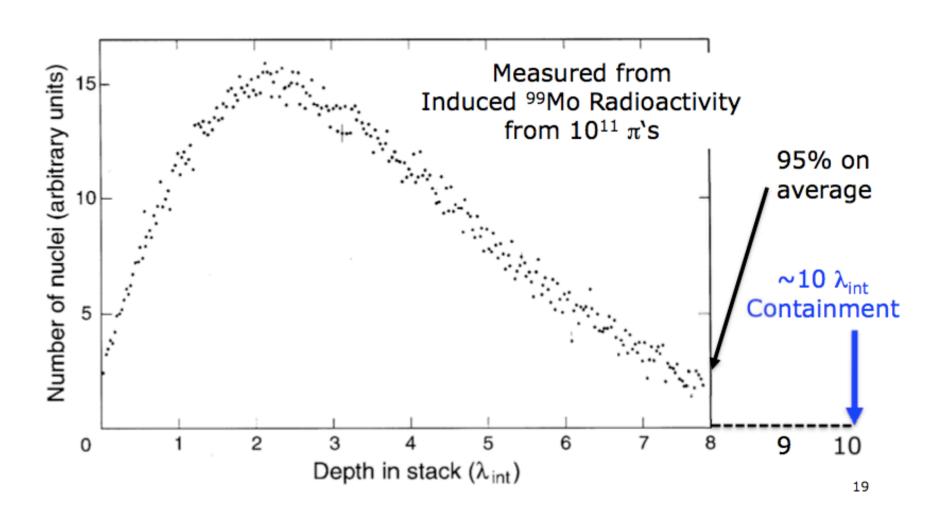
- ⇒ Visible energy systematically lower
- ⇒ Due to fluctuations in energy losses Energy resolution is worse than for electromagnetic calorimeters

Material Characteristics

Material	Z	Density [g/cm³]	X ₀ [cm]	λ _{int} [cm]	dE/dx _{mip} [MeV/cm]
Fe	26	7.9	1.8	17	11
Cu	29	9.0	1.4	15	13
Pb	82	11	0.6	17	13
w	74	19	0.4	9.6	22
²³⁸ U	92	19	0.3	11	21
Plastic Scint.	-	1.0	42	80	2.0
LAr	18	1.4	14	84	2.1
Quartz	-	2.3	12	43	3.9
Si	14	2.3	9.4	46	3.9
Al	13	2.7	8.9	39	4.4

Hadronic Shower

□ 300 GeV π ⁻ in Uranium

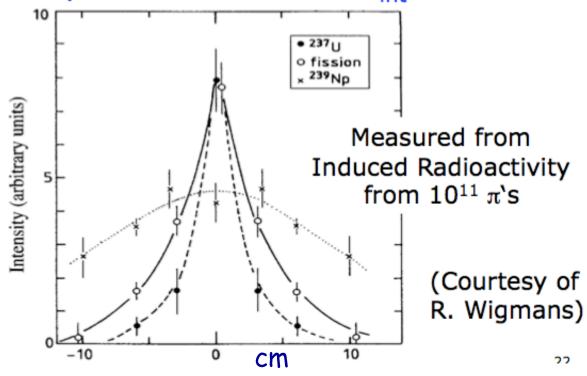


Hadronic Showers

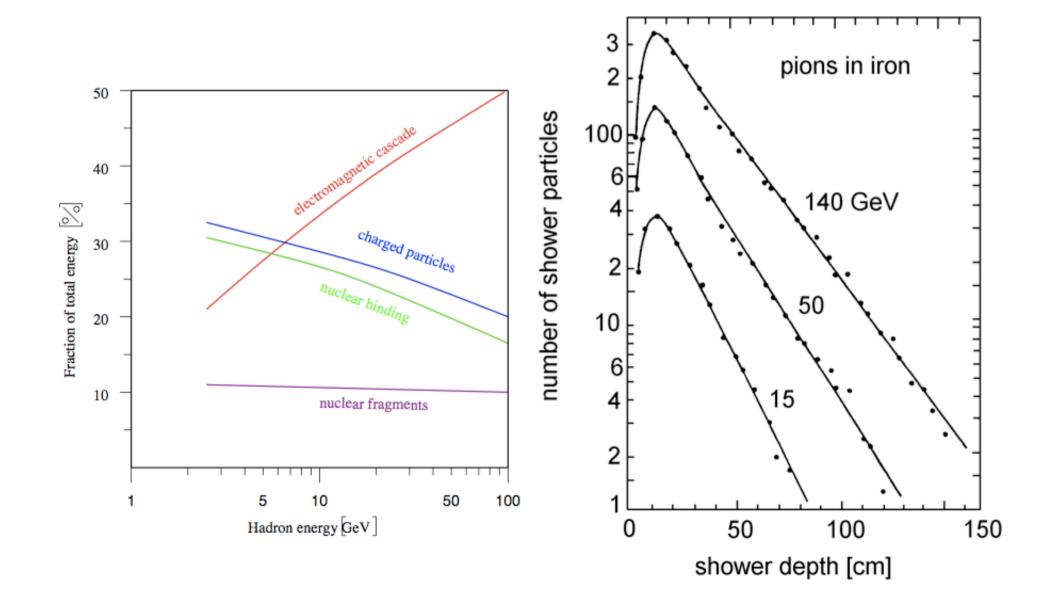
- What do we notice about hadronic showers besides the order of magnitude difference between X_0 and λ_{int} ?
 - 300 GeV π^- shower looks like an equiv. ~1 GeV electron shower in longitudinal profile with shower max at 2-3 λ_{int}
 - Multiplicity of interaction ∝ In s
 1 → N ~ 9 processes in the first λ_{int},
 dropping with In s to 1 → 6 in the second step,
 1 → 3 in the 3rd step, and
 then mainly 1 → 1 processes after that (shower max)
 - Also, recall π^0 's are falling out of the shower (at that energy) at a multiplicity fraction of 1/3 per interaction
- $\hfill\Box$ Another important feature of the pion is that it can remain a MIP for many λ_{int}
 - Although the probability drops off exponentially, there are many pions per event and many events to sort through

Hadronic Shower

- Transverse Profile is Shower Particle Species Dependent and Depth Dependent
 - Narrow EM core in the first few λ_{int}
 - Broad linear drop off after several λ_{int}
- More π^0 's γ' s in core
- Energetic neutrons and charged pions form a wider core
- Thermal neutrons generate broad tail



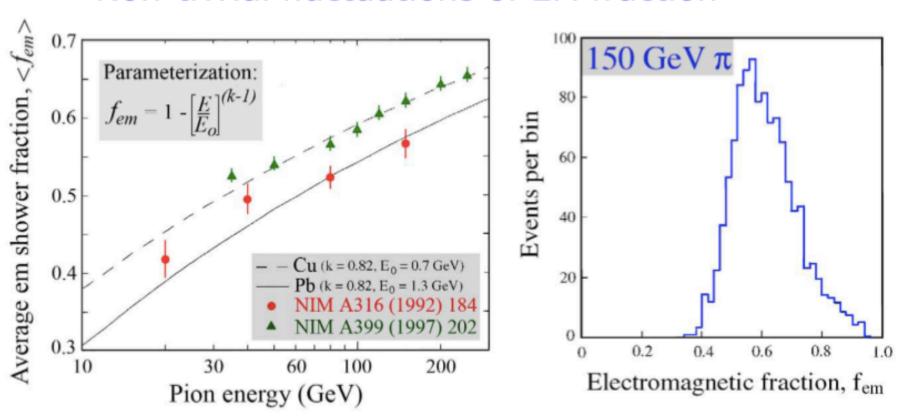
Hadronic Showers



EM Fraction of Charged Pion Showers

Growth of EM Fraction with Energy

Non-trivial fluctuations of EM fraction



Types of Calorimeters

- Particle showers are measured with (modern) fast, low-power instrumentation, but the adage is still true, what you see is what you get
 - One quickly finds that there are two major movements in the calorimeter world: the total absorptionists and the samplers
- A total absorption calorimeter is a (usually homogeneous) material in which the entire volume is sensitive to energy depositions
- A sampling calorimeter in an interleaving of absorber/dead material and active layers used to periodically sample the particle flow in the shower

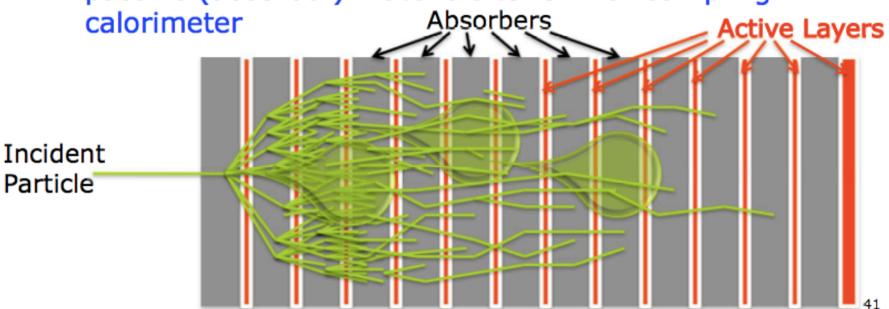
Total Absorption Calorimeter

- For a total absorption calorimeter, the stochastic term of the energy resolution is largely due to the counting statistics of light collection, but it's a little more involved:
 - Take PbW0₄ with ~100,000 photons/GeV, gives 0.3%
 - Apply the photodetection area and quantum efficiency of photodetector, now one has 4000 photoelectrons/GeV and 1.6%
 - Include the excess noise factor F=2 for amplification shot noise from the APD, $1.6\%*\sqrt{2}=2.2\%$
 - Now limit the lateral sum to keep the number of channels contributing to the electronic noise to 25, the containment fluctuations add 1.5% in quadrature, giving a total stochastic term of S=2.7%

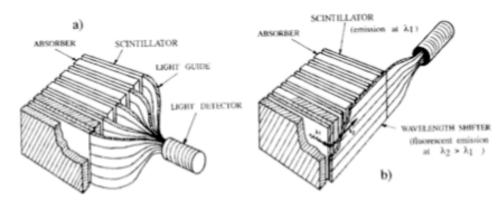
Sampling Calorimeters

- There are no known total absorption detectors that can stop hadronic showers (10λ_{int}) in a finite thickness (~few meters or less) and for finite cost
 - There are materials (Fe, Cu, Pb, W,²³⁸U) than can do this in 1-2 meters, but they are passive materials

One can therefore consider interleaving active and passive (absorber) materials to form a "sampling"



Sampling Calorimeters



Problem: How to choose thicknesses?

- Problems to consider:
 - Inactive part absorbs some of the produced shower particles, different for hadrons and electrons
 - Some part of hadronic response is lost due to neutron absorption
 - π⁰ → γγ: All hadronic showers have electromagnetic component, responses (physics effects) are different.

- Something "heavy", inactive: lead, uranium, iron (steel), ...
- Something "light", active: plastic scintillator, wire chamber, liquid (ionization chamber), . . .

Resolution for a Calorimeter

- The resolution of an energy measurement will depend on counting statistics of the quanta released by the active material and collected by a counting device
 - In a depleted solid-state detector (Si, Ge(Li)), an electron-hole pair can be liberated with ~3.8 eV on average (band gap of Si is 1.1 eV) with most of the deposited energy going into electron-hole pair creation
 - In a scintillator, visible light with energies 2-3 eV can be emitted for a given amount of energy deposition in the crystal (not all energy goes into light)

$$E(eV) = \frac{1240}{\lambda[nm]}$$

 A Cherenkov radiator, such as Lead-Glass or Quartz, will emit in the UV (~3-6 eV) for relativistic charged particles

Compensation

- Calorimeters can have greatly different efficiency for detecting electromagnetic as opposed to hadronic (mainly sensitive to MIP part) energy depositions
 - The ratio of the efficiencies is known as e/h
 - The "h" means the hadronic energy in a shower, not the energy from the shower of a hadron!
 - An incident charged pion will generate both electromagnetic and hadronic energy depositions in the calorimeter (EM fraction is energy dependent and fluctuates from shower-to-shower)
- Compensation means to design a calorimeter that has equal efficiency for both types of deposition e/h=1
 - We don't have this luxury anymore
 - Bunch crossings are too frequent to "wait" for neutrons

Project!

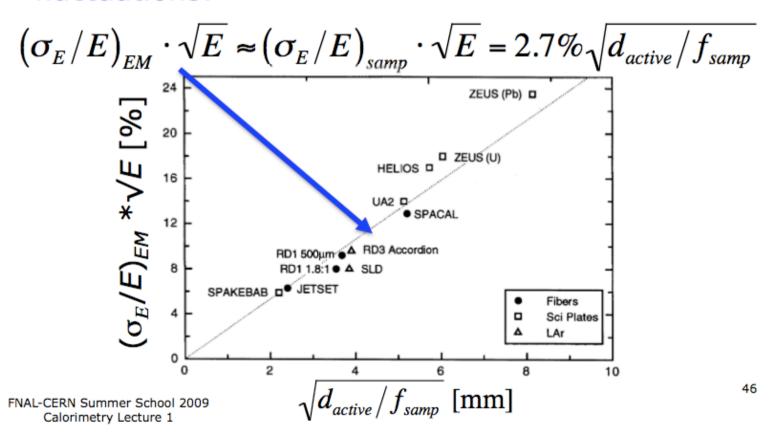
Can the EM and hadronic energies be measured separately for each shower?

Sampling Calorimeter Design

- Electromagnetic part was understood and good simulation software available (EGS)
- In the 1980's: First systematic studies for hadronic response
- First: Uranium / Scintillator. Very good resolution of first prototype.
- Idea was that fission gives back some of "lost" neutron energy.
- Later: By accident the first prototype was "compensated".
- mid-1980's: Systematic studies hadronic shower profiles, absorptions, by Wigmans et al.
- Result: One can tune any material combination to give identical responses to electrons and hadrons ("compensate"), due to different dependencies on Z of physics processes.
- Best resolution for hadrons only if calorimeter is compensated.
- Hadron resolution before: $\sigma_E/E \approx 100 \%/\sqrt{E}$
- Best hadron resolution achieved (ZEUS, SPACAL): $30 35 \% / \sqrt{E}$

Sampling Calorimeters

For EM showers in a sampling calorimeter, the energy resolution is dominated by the sampling fluctuations:



Sampling Calorimeter

- The relative size of the sampling fluctuation energy resolution term for hadronic showers can be estimated for similar calorimeter geometries from the relative thickness of the absorber layers in units of λ_{int}
 - For example, a calorimeter with a 45%/ \sqrt{E} stochastic term from hadronic shower sampling fluctuations would compare with a 80%/ \sqrt{E} resolution calorimeter with 3 times the absorber thickness t_{had} in units of λ_{int}

$$\sigma_E^{had\,,samp}(t_{had}=0.33)\big/\sigma_E^{had\,,samp}(t_{had}=0.11)\approx \sqrt{t_{had}^{rel}}=\sqrt{3}$$

	X ₀ (cm)	$\lambda_{\rm int}({ m cm})$
Pb	0.56	17.0
PbWO ₄	0.89	18.0
Fe	1.76	16.8
Cu	1.43	15.1

	† _{em}	† _{had}
ATLAS, Tilecal (Fe)	1.0	0.11
CMS HCAL (Cu)	3.5	0.33

47

Sampling Calorimeters

- However, sampling fluctuations are not the whole story, and several other terms contribute to the energy resolution. Other contributions include:
 - Visible Energy Fluctuations (Nuclear Binding Energy and Escaping Neutrons)
 - Electromagnetic Fraction Fluctuations (for noncompensating calorimeters)
 - Containment (Longitudinal and Lateral) Fluctuations
 - Electronic Noise (at low Energy)
 - Counting Statistics of Signal Quanta (for very low yield active layers)
 - Excess Noise Factor in the Gain Mechanism of the Signal Quanta Detector
- Tevatron/LHC calorimeter examples will be covered in Lecture 2

CMS: Calorimeters

ECAL: Barrel 36 super modules/1700 crystals Endcaps detectors completed in summer 2008 Total of ~75000 crystals for this detector



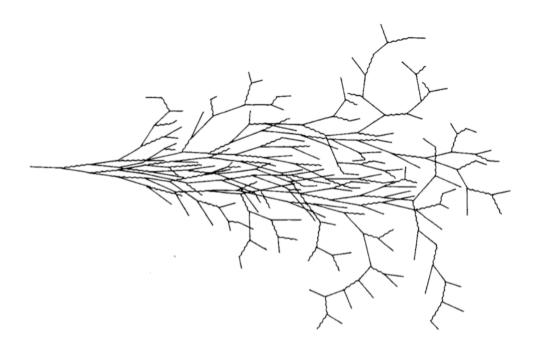
Central ECAL installation in CMS

Hadronic Calorimeter (brass/scintillator) completed in 2006
Lowering in the experimental hall

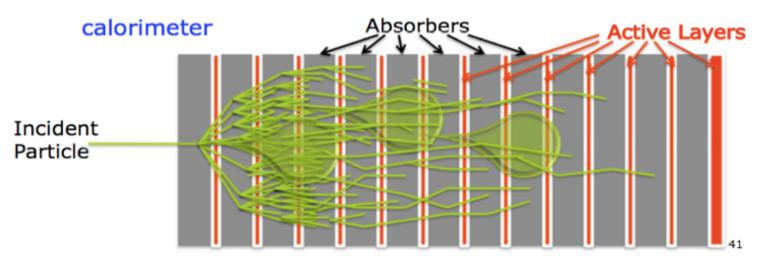




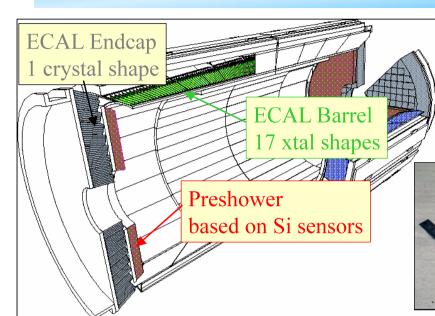
Showers & Calorimeters...



Total absorption calorimeter or sampling calorimeter



The Electromagnetic Calorimeter



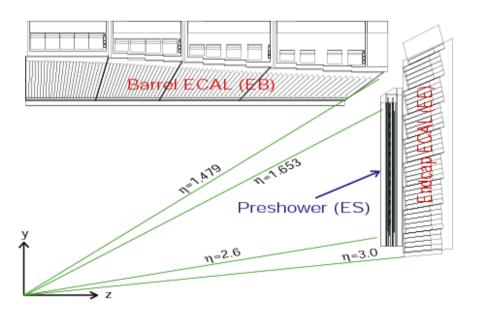
Characteristics of PbWO₄

 $X_0 = 0.89$ cm

 $\rho = 8.28 \text{g/cm}^3$

 $R_{\rm M}$ (Molière radius) = 2.2cm

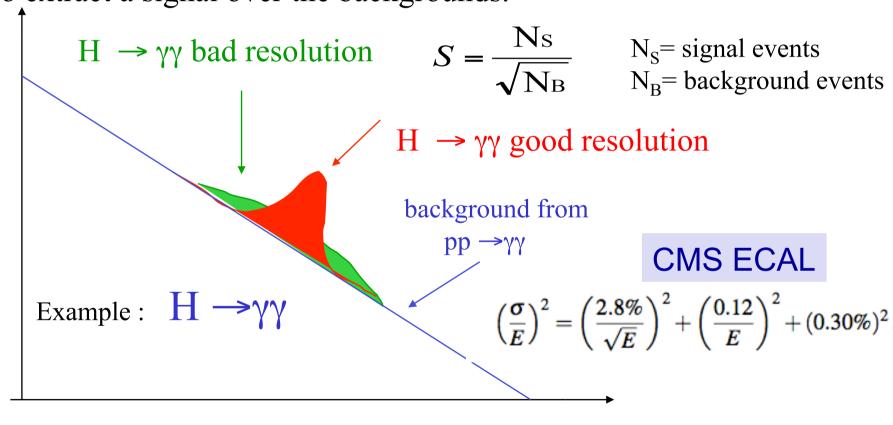




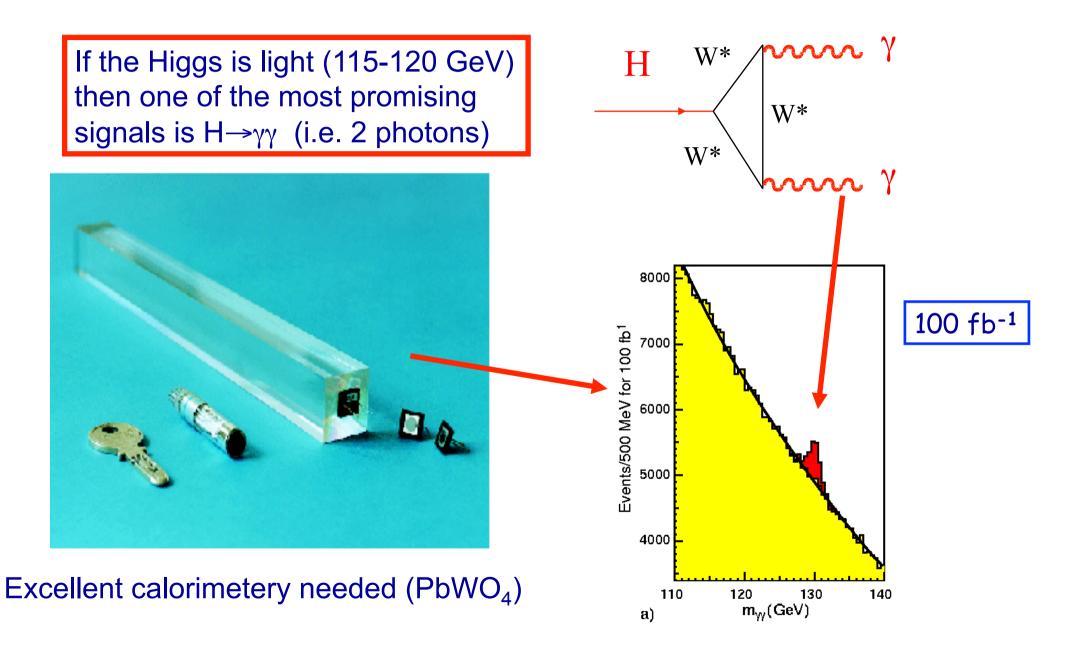
Parameter	Barrel	Endcaps
Coverage	ΙηΙ<1.48	1.48 <lηl<3.0< td=""></lηl<3.0<>
Δφ 🗴 Δη	0.0175 x 0.0175	0.0175 x 0.0175 to 0.05 x 0.05
Depth in X ₀	25.8	24.7
# of crystals	61200	14648
Volume	8.14m ³	2.7m ³
Xtal mass (t)	67.4	22.0

Calorimeter Resolution: eg. for Higgs

• Excellent energy resolution of EM calorimeters for e/γ and of the tracking devices for μ in order to extract a signal over the backgrounds.

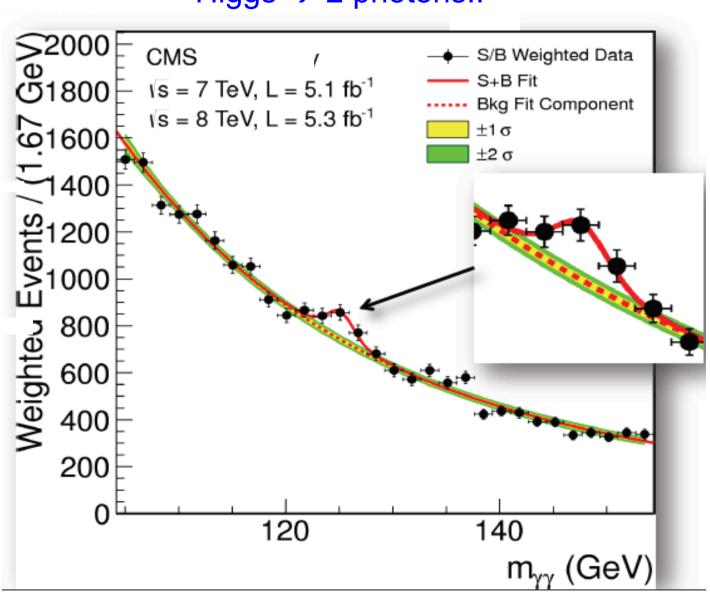


CMS: Lead Tungstate EM Calorimeter

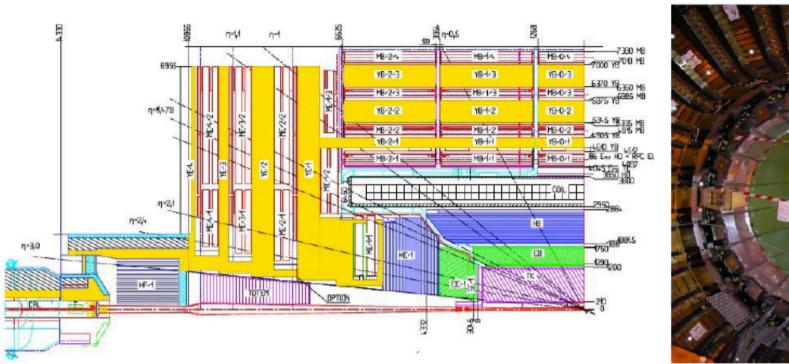


Higgs Search Results

Higgs → 2 photons!!



Hadron Calorimeter

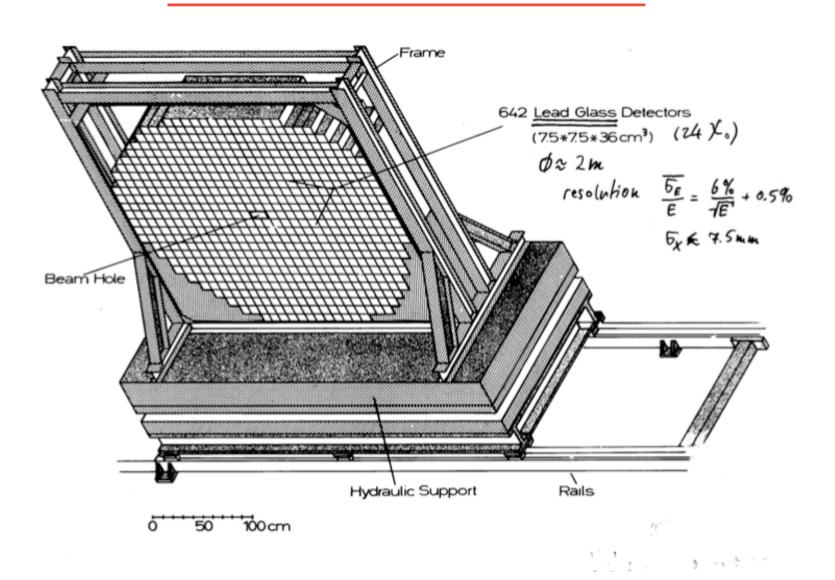




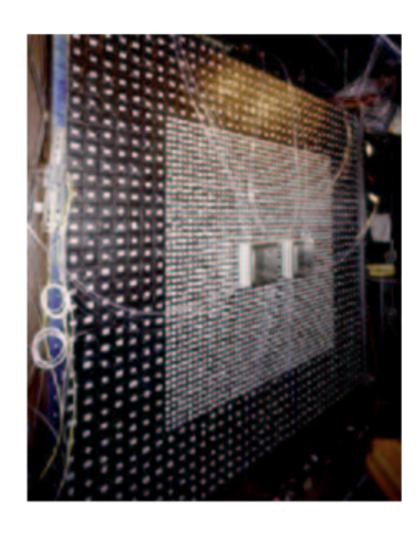
- Scintillator-brass/steel tile calorimeter: compact, hermetic, good segmentation and coverage (|η|<5.2)
- Jet angular resolution ~ 20 (30) mrad in φ (θ) at E_T ≥ 100 GeV

Energy resolution HCAL+ECAL $\Delta E/E \approx 100\%/\sqrt{E} \oplus 5\%$

Lead Glass Calorimeter (WA79)



CsI Crystals (KTeV)

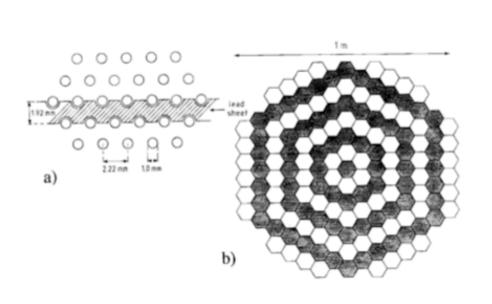


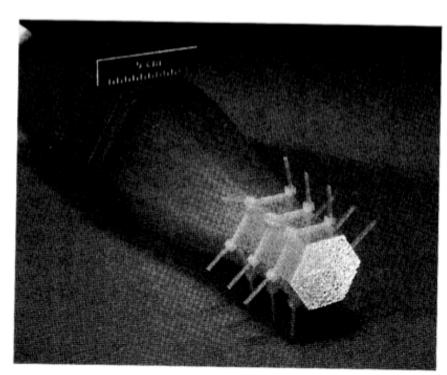
 $3100~\mathrm{CsI}$ crystals



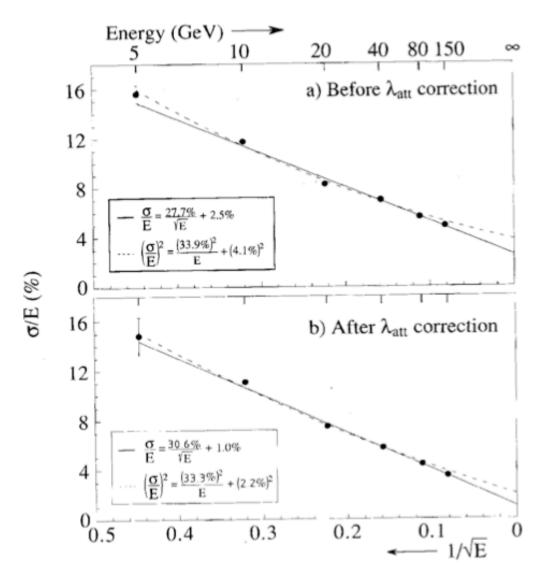


Spaghetti Calorimeter (SpaCal)





Spacal Resolution



R. Wigmans, Colorimetry (Oxford Science, 2000)

Particle Identification

Particle Idenfication

- Identification of neutral particles
- Identification of charged particles

Neutral particles

- Measure total energy (Calorimeter)
- If no charged track points to signal in Calorimeter: It's a neutral
- Usually not too many possibilities left.
 Example: Hadron calorimeter, no track: most likely a neutron (or K_L⁰)
- Electromagnetic calorimeter, track, signal: Measure "E/p". E/p = 1 for electrons, E/p < 1 for pions
- Long-lived neutral particles (Hyperons), short lived particles (charm, beauty):
 Measure 4-vector of decay products and calculate invariant mass.

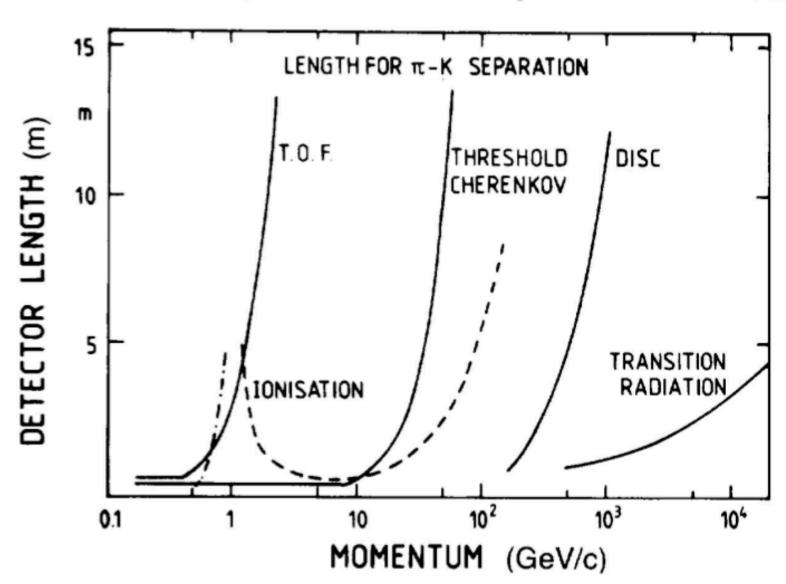
Radiation of Charged Particles

Radiation is emitted by a charge particle if:

- 1. v > c/n: Cherenkov radiation
- 2. $\vec{v}/c_{\rm ph} = \vec{v} \cdot n/c$ changes
 - (a) $|\vec{v}|$ changes: Bremsstrahlung
 - (b) direction of \vec{v} changes: Synchrotron radiation
 - (c) n changes: Transition Radiation

Particle Idenfication

Fig. 5.30. Length of detectors needed for separation of π and K mesons.



Time of Flight

- Put two Scintillation Counters at a known distance
- Measure time difference between the two signals

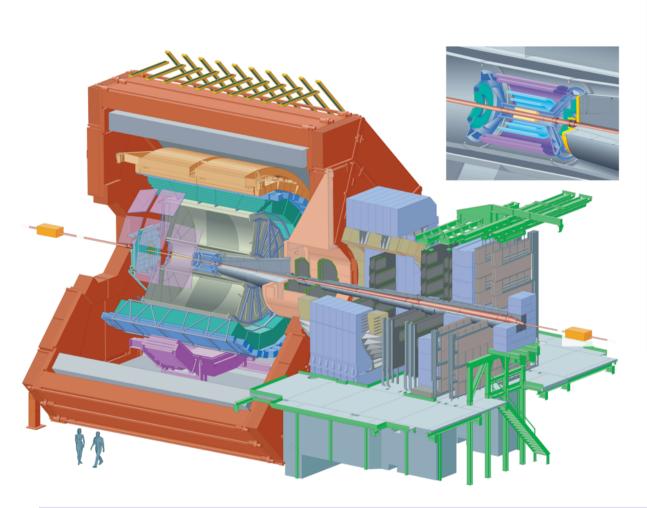
Good time resolution: 150 psec.

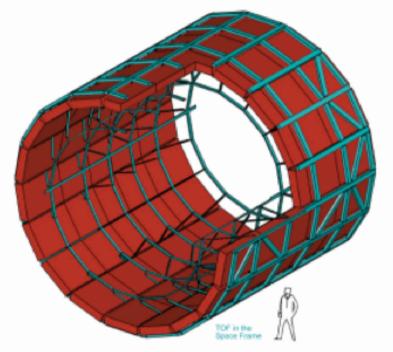
Maximum distance: $\approx 10 \,\mathrm{m}$ (detector), $\approx 100 \,\mathrm{m}$ (beamline).

 \Longrightarrow Can measure difference between Kaons and Pions up to a few GeV/c

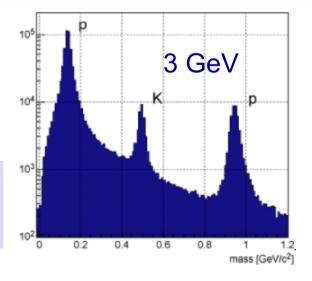
Also has problem at higher rate and/or multiple particles hitting the same scintillator

Time of Flight in ALICE





Fast RPC detectors: 50-100 ps time resolution Identify particles in range 2-4 GeV



Transition Radiation

Transition Radiation: Reformation of particle field while traveling from medium with $\epsilon = \epsilon_1$ to medium with $\epsilon = \epsilon_2$.

Energy of radiation emitted at a single interface

$$S = \frac{\alpha \hbar z^2}{3} \frac{(\omega_1 - \omega_2)^2}{\omega_1 + \omega_2} \gamma$$

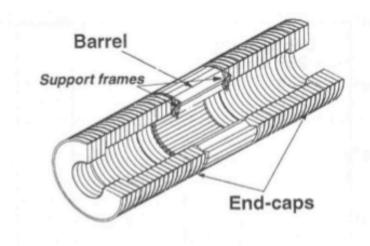
 $\alpha = 1/137$, ω_1 , ω_2 plasma frequencies, $\gamma = E/mc^2$. Typical values: Air $\omega_1 = 0.7 \,\text{eV}$, polypropylene $\omega_2 = 20 \,\text{eV}$

Spectral and angular dependence of Transition Radiation:

$$\frac{d^2}{d\vartheta d\omega} = \frac{2e^2}{\pi c} \left(\frac{\vartheta}{\gamma^{-2} + \vartheta^2 + \omega_1^2/\omega^2} - \frac{\vartheta}{\gamma^{-2} + \vartheta^2 + \omega_2^2/\omega^2} \right)^2$$

 \implies Most of radiation in cone with half angle $1/\gamma$: forward in particle direction.

Transition Radiation Detector



Length:	Total	6802 cm	N straws:	Total	372032
	Barrel	148 cm		Barrel	52544
	End-cap	257 cm	and the same	End-cap	319488
Outer dia	meter	206 cm	N electroni	cs channels	424576
Inner diameter		96-128 cm	Weight	~ 1	500 kg

Fig. 11. ATLAS Transition Radiation Tracker (TRT) conceptual design [2].

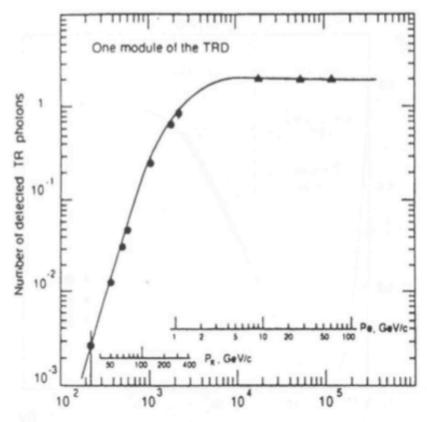


Fig. 8. The detected number of the TR photons for different Lorentz factors [4].

Cherenkov Radiation

A charged particle with a velocity v larger than the velocity of light in a medium emits light.

Angle of emission:
$$\cos\theta_c = \frac{1}{\beta\,n} = \frac{1}{\frac{v}{c}\,n}$$
 Number of photons:
$$\frac{d^2N}{dEdl} = \frac{\alpha z^2}{\hbar c} \left(1 - \frac{1}{(\beta n)^2}\right) = \frac{\alpha z^2}{\hbar c} \sin^2\theta_c$$

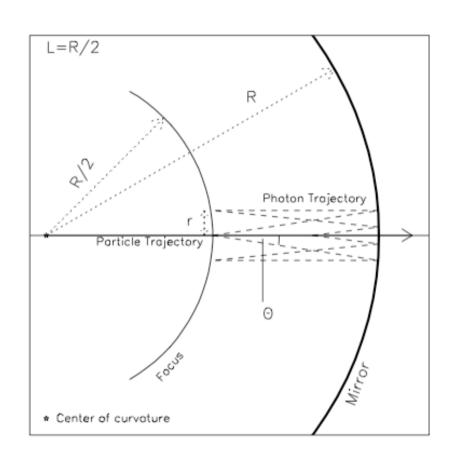
$$\frac{d^2N}{d\lambda dl} = \frac{2\pi\alpha z^2}{\lambda^2} \sin^2\theta_c$$

First (obvious) application: Threshold Cherenkov Detectors

For fixed momentum and only 2 particles to separate (beam line)

More than 2 particles and/or wider momentum range: Several counters at different thresholds

Ring Imagine Cherenkov



$$\cos \theta_c = \frac{1}{\beta \cdot n}$$

$$r = F \cdot heta_c = rac{R}{2} \cdot heta_c$$

$$N_{ph} = N_0 \cdot L \cdot \sin^2 \theta_c$$

 θ_c : Cherenkov angle

 β : velocity

n: refractive index

r: Radius of ring on focal surface

R: Radius of curvature of spherical mirror(s)

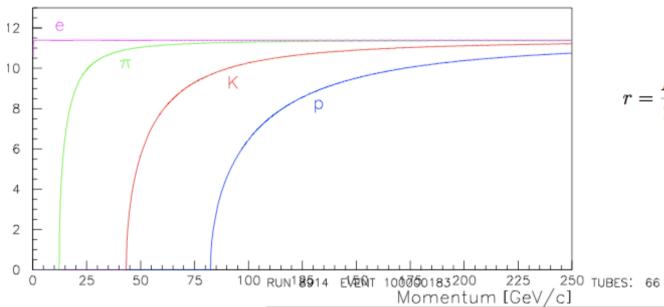
F: Focal length (F = R/2)

L: Radiator length (usually L = F)

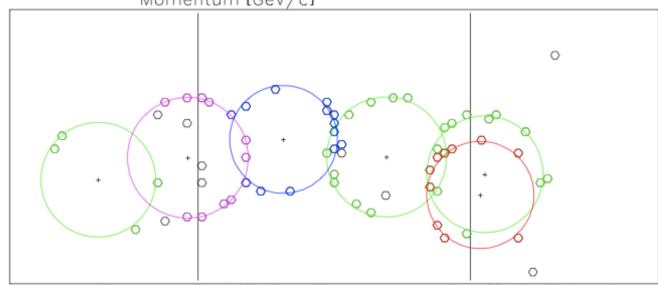
Parallel particles have the same ring image

Ring Imagine Cherenkov

Cherenkov Radii - Neon Radiator, F= 1000cm

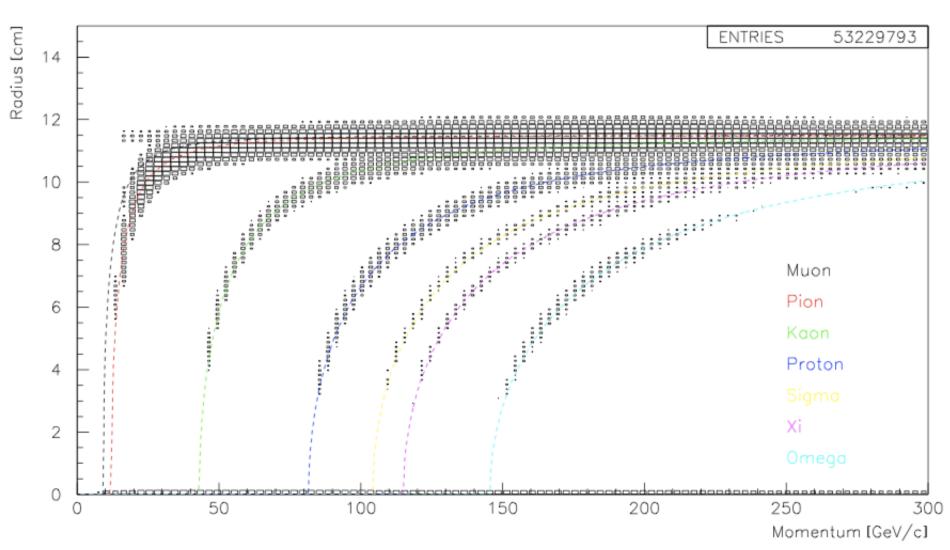


$$r = \frac{R}{2} \sqrt{2 - \frac{2}{n} \sqrt{1 + \frac{m^2 c^2}{p^2}}}$$



Ring Imagine Cherenkov

SELEX RICH: Particle Id negative tracks



RICH

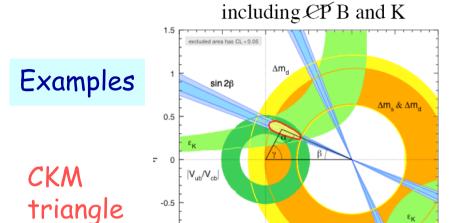
- Center of ring depends on track angle \Longrightarrow large detector surface (up to square meters)
- good resolution of photon position ⇒ large number of "pixels" (up to 100000 or more)
- Spectrum of Cherenkov photons

$$\frac{dN}{d\lambda} = \frac{2\pi\alpha}{\lambda^2} L \sin^2\theta_c$$

⇒ Ultraviolet

- refractive index $n = n(\lambda) \Longrightarrow$ Chromatic dispersion
- Detection of UV-photons: convert photon in electron (photoeffect)
 - 1. small (up to a few thousand) number of pixels: Photomultipliers
 - 2. large number of pixels or area: Time Expansion Chambers with TEA or TMAE
- When using TEC: particle pass through the chambers: dE/dx
- When using TEC: response (memory) time limit rate

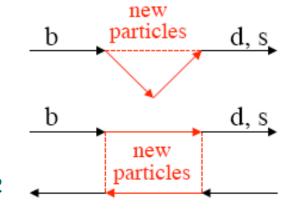
LHCb: b-physics at the LHC



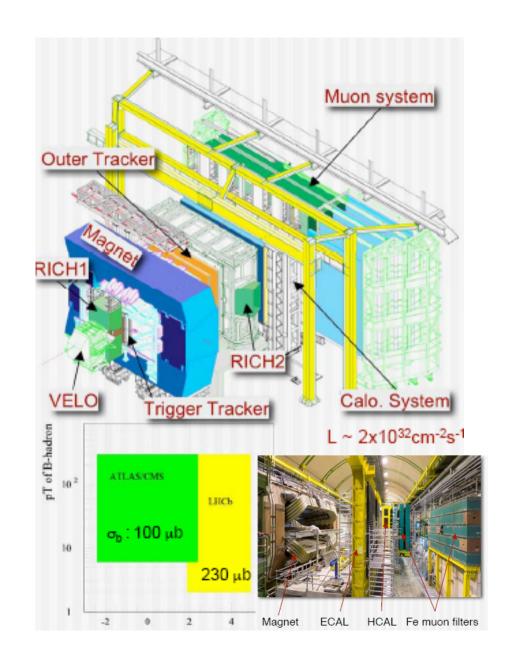
CKM fitter group 2004

 $B_s \rightarrow J/\psi \phi$ 120k signal events/year in LHCb $\sigma(\sin\phi_s) \sim 0.06$, $\sigma(\Delta\Gamma_s/\Gamma_s) \sim 0.02$

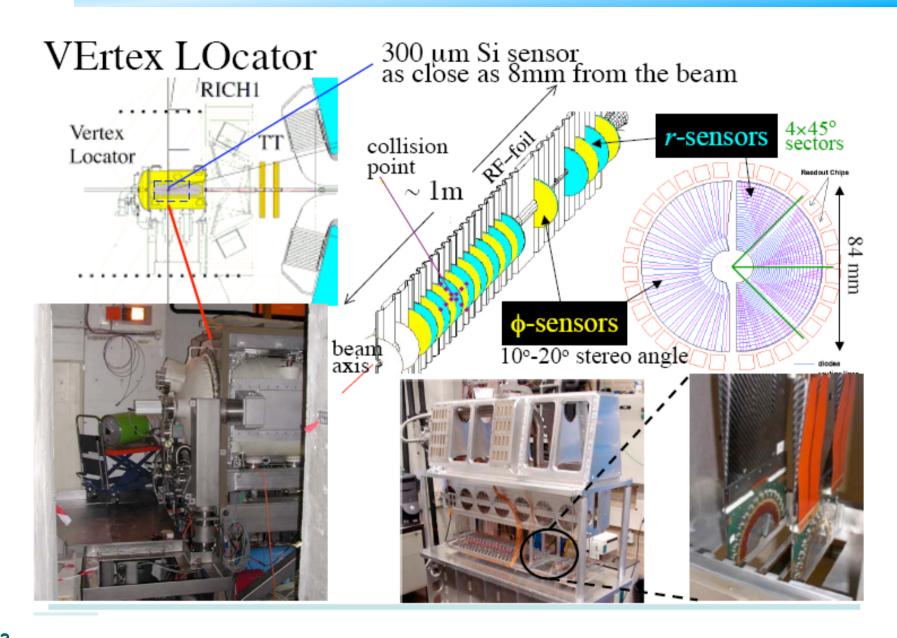
Measurement of $B_s - \overline{B}_s$ oscillation



Sensitive to new physics complementary to ATLAS/CMS



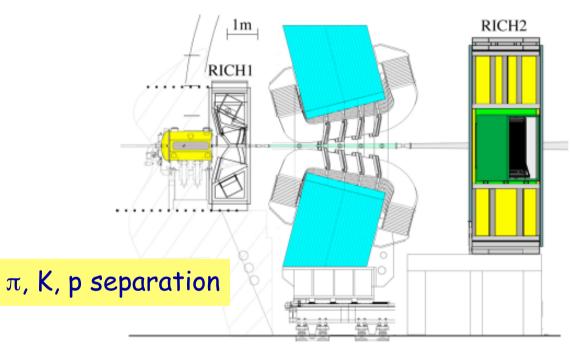
VErtex LOcater



LHCb Particle Identification

Based on cherekov light emission

RICH Ring Imaging Cherenkov

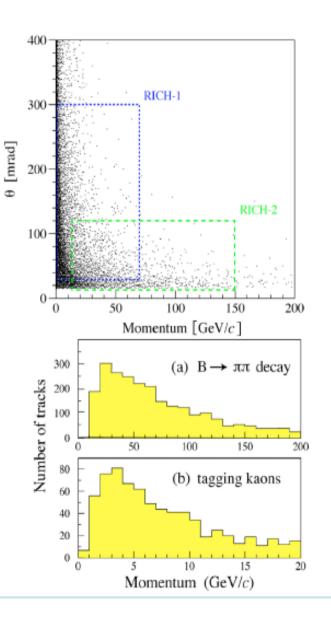


Two RICH with three radiators

 $\begin{array}{c}
\text{Aerogel} \\
\text{C}_4\text{F}_{10}
\end{array}$ R CF_4 R

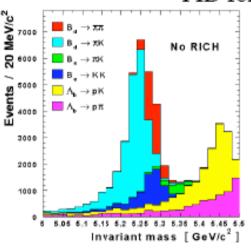
RICH1 (25-300 mrad)

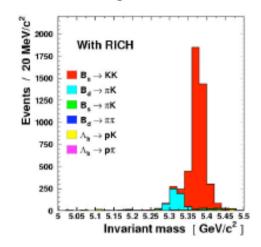
RICH2 (15-120 mrad)

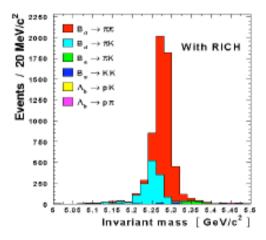


Particle Identification

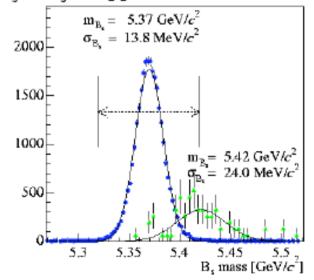
PID for $B \rightarrow \pi\pi$ and $B_s \rightarrow KK$ reconstruction

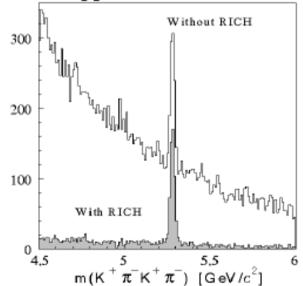






 $B_s \rightarrow D_s \pi$ suppression with PID for $B_s \rightarrow D_s K$ Comb. suppression with PID for $B \rightarrow DK^{*0}$





Summary Particle Identification (cont.)

	tracking chamber		renkov cou		electromagn	n. hadron calorimeter	muon chambers	
~	Chamber	n ₁ <	c n ₂	< n ₃	Talorimeter		CHAITIBETO	1
γ ~~~								
e^+,e^-	xxxxxxxx	~~~	Lord	کریر دریر	X			
μ^{+},μ^{-}	xxxxxxxx		}	~~~~	xxxxxx	xxxxxx	xxxxxxxx	→µ
π^+,π^-	xxxxxxxx		^ڳ وڻ	Are son	xxxxxx	xx 🔄		
	xxxxxxxx			~~~~	xxxxxx	xx 🚓		
_n						*		
_v								→v

END