Theory versus Experiment

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Vrije Universiteit Brussel

Theory versus Experiment



Dangerous cocktail !!!



The basics in these lectures

Part1 : "Theory meets experiment"

- ① Our QFT description of Nature is a stochastic one
- ② General stochastic distributions in physics
- ③ From theoretical to experimental distributions
- ④ ... and back: unfolding techniques
- 5 Examples from the LHC at CERN

Part 2 : "Experiment meets theory"

- ① Experimental aspects to accumulate experimental data
- ② Selection of the dedicated signal
- ③ Performing measurements & parameter estimation
- ④ Claiming a discovery of new physics or setting limits
- 5 Examples from the LHC at CERN

Lecture 1

Theory versus Experiment - Experimental Techniques in Particle Physics - Jorgen D'Hondt (Vrije Universiteit Brussel)

"Theory meets experiment"

- 1 Stochastic description of Nature Stochastic variables, distributions, examples
- ② General stochastic distributions in physics Bernouilli, Binomial, Poisson, Gaussian, Central Limit Theorem
- ③ From theoretical to experimental distributions Nuisance of experiment, convolution, Monte Carlo simulation, some reconstruction techniques
- ④ A basic introduction to unfolding techniques
- ⑤ An example from the LHC at CERN

Deterministic vs Stochastic

Particles through an electromagnetic field (example a photonmultiplier tube)

$$\vec{F} = q \cdot \left(\vec{E} + \vec{v} \times \vec{B}\right)$$

Deterministic Each "experiment" is predictable (exact)



Set of "experiments" is predictable (distributions)

Be aware that large systems are difficult to model with a deterministic equation, hence stochastic models are used predicting general parameters of the system ...

Think about your lectures on Statistical Physics

The micro-scale Nature is stochastic!

• Fundamental interactions are described on the level of quantum mechanics which is stochastic. Quantum Field Theory predicts cross-sections and distributions of kinematic variables.



 Prediction of the <u>expected</u> amount of events observed in collisions and the <u>expected</u> kinematic distributions. But not the prediction of the exact result of one single experiment.

Distributions of stochastic variables

- A stochastic variable X denotes the outcome of one experiment and usually obtains a real value (ℝ) after its measurement.
- When repeated infinite times in the same conditions, a distribution is obtained (can be discrete or continuous).



Distributions of stochastic variables

- The collection of momenta $\{\mu_k(X)|k=\{1...\infty\}\}$ gives a full description of the distribution $f_X(x)$
- Most distributions in physics have only few free momenta (the others are zero or can be expressed in terms of other momenta)
- Definition of expectation value: $E[g(X)] \equiv \int_{\Omega} g(x) f_X(x) dx$ Typical examples of theoretical parameters of a distribution:

$$\mu_X \equiv \mu_1(X) = E[X^1] = \int_{\Omega} x^1 f_X(x) dx Var[X] \equiv E[X^2] - (E[X])^2 = \int_{\Omega} (x - E[X])^2 f_X(x) dx$$

These parameters are unknown and have to be measured

Examples of stochastic variables (X): number of collision events in a dataset of 1/fb, reconstructed value of $m_{t\bar{t}}$ per event, ...

Distributions in physics

Which distributions are relevant to compare theory with experiment in particle physics?

Binomial distribution

Starts from a very simple Bernouilli distribution: the stochastic variable can only take two values (A or B)



Pag.

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Binomial distribution

• One parameter to describe the full distribution P(i): N (number of Bernouilli experiments)



$$(x+y)^N = \sum_{i=0}^N \frac{N!}{(N-i)!i!} x^i y^{N-i}$$

 $P_N(i) = \frac{N!}{(N-i)!i!} p^i (1-p)^{N-i}$
 $\mu_X = E[X] = N.p$
 $Var[X] = N.p.(1-p)$

p = probablity for result A (eg. ball goes left)

Binomial distribution

- Typical exercise:
- A particle detector has an efficiency of 90% per detector layer. How many detector layers do we need to put on top of each other to get a probability of 99% to detect the particle? Detecting the particle means, that we have to "see" the particle in at least 3 layers.



Gaussian distribution

 The most important distribution in physics is the Gaussian one which is a rescaling of a binomial stochastic variable X ~ B(n,p)

$$Z = \frac{X - n \cdot p}{\sqrt{n \cdot p \cdot (1 - p)}} \xrightarrow{n \to \infty} f_Z(z) = \frac{1}{\sqrt{2\pi}} exp(-\frac{1}{2}z^2)$$



Poisson distribution

Stochastic variable X describes how many events happen in a fixed time interval (eg. how many collisions in 1/fb)



Central Limit Theorem

Consider independent stochastics X_i following all a random distribution $f_{Xi}(x_i)$. Each stochastic variable Y being a linear combination of these

 $Y = \sum_{i=1}^{n} c_i X_i$

Will follow a normal distribution (when the variance Var[Y] is not dominated by one variance $Var[X_i]$).

$$Y_{n \to \infty} N\left(\sum_{i=1}^{n} c_i E[X_i], \sum_{i=1}^{n} c_i^2 \sigma_{x_i}^2\right)$$

Hence the theory of uncertainties can be developed assuming the measurable stochastic follows a Gaussian distribution.



Gaussian distribution

Estimators are usually linear combinations of stochastic variables, hence follow a Gaussian distribution



Central Limit Theorem

The distributions X_i should not have the same PDF:



Our particle detectors are typically complex instruments where particles are reconstructed from several "hits" which are combined into estimators for the four-momentum of the particle.

 \rightarrow Gaussian resolution functions

Response & resolution

If I put in my detector a particle with variable value $X=x_{in}$, I will observe it at another value X=x' according to some distribution.



Stochastic effects from

- 1) the detector granularity
- 2 the detector instrument
- ③ the physics (eg. jet reconstruction)

Resolution functions

1 the detector granularity

Detectors make our life more complicated, but are needed!



Resolution functions ① the detector granularity

Detectors make our life more complicated, but are needed!



Resolution functions 1 the detector granularity

Detectors make our life more complicated, but are needed!



The more granular the detector, the more expensive the detector!

Resolution functions 2 the detector instrument

Physics itself can smear the "true" direction or energy of a particle



The incoming direction or energy is altered in a stochastic way and the <u>expected behavior</u> can be described by models put in the simulation of collision events at particle detectors.

Resolution functions

granularity + instrument + physics

The resolution function describes the stochastic distribution of the observable variable X (eg. p_T) for fixed settings before the measurement.



One can reflect both the variance (resolution) and the bias (response) of the estimator into a <u>response matrix</u>.

Response matrix

The response matrix from MC simulation



matrix R_{ii} = Prob(obs in bin i | true value in bin j)

From TH to EXP distributions

Most of the resolution functions R(X,X') are Gaussian

$$R(X, X') = \frac{1}{\sqrt{2\pi\sigma^2}} exp\left(-\frac{1}{2}\left(\frac{x-x'}{\sigma}\right)^2\right)$$

and reflect the stochastic aspect of the measurement of X' given the initial "true" value X.

Hence the measured distribution becomes ("convolution")

 $g(x') = \int R(x, x') f_X(x) dx$

It is the distribution g(x') which is sampled by the experiment. Including physics $(\vec{\theta})$ and detector "nuisance" $(\vec{\alpha})$ parameters:

$$g(x'|\vec{\alpha}, \vec{\theta}) = \int R(x, x'|\vec{\alpha}) f_X(x|\vec{\theta}) dx$$

From TH to EXP distributions

$$g(x'|\vec{\alpha}, \vec{\theta}) = \int R(x, x'|\vec{\alpha}) f_X(x|\vec{\theta}) dx$$

We want to know something about the physics model $f_X(x|\theta)$ using a finite amount of measurements of stochastic variable X'.

The data of the measurements will be collected into a histogram with a finite amount of bins. In general two options:

- (1) With simulation which incorporates the stochastic behavior of the response matrix R, we can predict the expectation value in each bin (= the bin content). And compare the data histogram with these expectations which depend on the parameter θ .
- 2 When the response matrix R is well-known we can try to inverse the problem and estimate directly $f_{X}(x|\theta)$.

("inverse problem")

Estimating probability distributions $f_Y(y)$ with an additional stochastic effect on Y from the measurement process (effect of R), in case when no parametric form is available



"histograms"
$$E[n_i] \equiv \nu_i = \sum_{j=1}^M R_{ij} \mu_j \rightarrow E[\vec{n}] = \vec{\nu} = \tilde{R}\vec{\mu}$$

 $\sum_{j=1}^N R_{ij} = Prob(obs anywhere | true value in bin j) = \varepsilon_j (efficiency)$

With pictures...

$$\rightarrow E[\vec{n}] = \vec{\nu} = \tilde{R}\vec{\mu}$$



Take care of the background $E[\vec{n}] = \vec{\nu} = \tilde{R}\vec{\mu} + \vec{\beta}$





• Now we should invert the equation to estimate $\ ec{\mu}
ightarrow ec{\mu}
ightarrow ec{\mu}$

$$E[\vec{n}] = \vec{\nu} = \tilde{R}\vec{\mu} + \vec{\beta} \qquad \Rightarrow \qquad \vec{\mu} = \tilde{R}^{-1} \cdot (\vec{\nu} - \vec{\beta})$$

- Suppose every n_i has a Poisson distribution, then the maximum likelihood estimator of $\vec{\nu}$ is simply the observed \vec{n}

$$P(n_i|\lambda = \nu_i) = \underbrace{\frac{\nu_i^{n_i}}{n_i!} e^{-\nu_i}}_{\left(\frac{\partial \mathcal{L}(\nu_i|n_i)}{\partial \nu_i}\right)_{\nu_i = \hat{\nu}_i}} = 0 \qquad \Rightarrow \quad \hat{\nu}_i = n_i$$

- Hence we have $\hat{\vec{\mu}} = \tilde{R}^{-1} \cdot (\vec{n} \vec{\beta})$
- One can show that this estimator is the most efficient one (i.e. with the smallest variance) among all unbiased estimators
- But...

- Using the simple equation $\hat{\vec{\mu}} = \tilde{R}^{-1} \cdot (\vec{n} \vec{\beta})$
- We get a dramatic effect...



x 10²

"true" distribution

observed distribution

- Huge fluctuations because of the fluctuations of $ec{n}$ around $ec{
 u}$
- Introduce some bias (systematic uncertainty) to reduce the variance (statistical uncertainty) → <u>regularized unfolding</u>

Regularized Unfolding

Still use the same master equation $\hat{\vec{\mu}} = \tilde{R}^{-1} \cdot (\hat{\vec{\nu}} - \vec{\beta})$ But adapt the Likelihood in the Maximum Likelihood method

$$ln\mathcal{L}(\vec{\nu}|\vec{n}) \longrightarrow ln\mathcal{L}'(\vec{\nu}|\vec{n}) = \alpha ln\mathcal{L}(\vec{\nu}|\vec{n}) + S(\vec{\nu})$$

with α is the regularization parameter and S(μ) the regularization function. Hence $\hat{\vec{\nu}} \neq \hat{\vec{\nu}}_{MaxLik} = \vec{n}$, but the solution of

$$\left(\frac{\partial ln\mathcal{L}'(\nu_i|n_i)}{\partial \nu_i}\right)_{\nu_i=\hat{\nu}_i} = 0 \quad \longrightarrow \quad \hat{\nu}_i = \dots$$

Different options for the regularization parameter and function. Examples in eg. arXiv:hep-ex/0208022 and arXiv:1104.2962
Regularized Unfolding

$$ln\mathcal{L}(\vec{\nu}|\vec{n}) \longrightarrow ln\mathcal{L}'(\vec{\nu}|\vec{n}) = \alpha ln\mathcal{L}(\vec{\nu}|\vec{n}) + S(\vec{\nu})$$

The <u>regularization function</u> needs to smoothen the likelihood. Therefore a good choice could be the mean square of the second derivative. $S(\vec{x}) = \sum_{n=1}^{N-2} (n + 1)^2$

$$S(\vec{\nu}) \sim \sum_{i=1}^{N-2} (-\nu_i + 2 \cdot \nu_{i+1} - \nu_{i+2})^2$$

This is related to the amount of curvature in the expectation value of $\vec{\nu}$ versus the measurant X.

The value for the <u>regularization parameter</u> is a trade-off between variance and bias. Hence it can be chosen to minimize both simultaneous.

MSE =
$$\frac{1}{N} \sum_{i=1}^{N} (Var[\hat{\mu}_i] + \hat{b}_i^2)$$
 with $b_i = E[\hat{\mu}_i] - \mu_i$

Alternative to unfolding

• Using simulations a simple method exist with multiplicative correction factors.

$$\hat{\mu}_i = C_i (n_i - \beta_i) \qquad C_i = \frac{\mu_i^{MC}}{\nu_i^{MC}}$$

simple method does not take into account all correlations

• The bias of the estimator is

$$b_i = \left(rac{\mu_i^{MC}}{
u_i^{MC}} - rac{\mu_i}{
u_i^{sig}}
ight)
u_i^{sig} \quad (
u_i^{sig} =
u_i - eta_i)$$

Only no bias if the MC simulated model is correct, and the estimators are pulled towards the MC model used for the correction factors $C_i \dots$ not good! \rightarrow simply compare \vec{n} directly with $\vec{\nu}$



Why unfolding ?

- ① Comparison between experiments
- ② Comparison with new theories (or other theories which experimentalists have not considered)

Unfolding in ROOT: RooUnfold (arXiv:1105.1160)

Examples from the LHC

arXiv:1207.0065

The charge asymmetry A_C in top quark pair events:

$$A_C = \frac{N^+ - N^-}{N^+ + N^-}$$

where N^{+/-} reflects the amount of events for which $\Delta |y| = |y_t| - |y_{\bar{t}}|$ is either positive or negative.



Addendum: Rivet

http://rivet.hepforge.org/

"Rivet is a library and set of programs which produce simulated distributions which can be directly compared to measured data for MC validation and tuning studies. It can also be used without reference data to compare two or more generators to each other for regression testing or tune comparison. The Rivet library contains the tools needed to calculate physical observables from HepMC files or objects, a large set of important experimental analyses, and histogramming tools for data comparison and presentation."

Summary of part 1

Summary of part 1

Theory needs to meet experiment!

1 Nature at the quantum level is stochastic ... deal with it!

(2) Fundamental physics is reflected in distributions $f_{\chi}(x|\theta)$

③ Detector nuisance effects: $g(x'|\vec{\alpha}, \vec{\theta}) = \int R(x, x'|\vec{\alpha}) f_X(x|\vec{\theta}) dx$

(4) The distributions $g(x'|\vec{lpha}, \theta)$ are measurable

(5) Unfolding techniques can give you $f_X(x|\theta)$ back...

Lecture 2 – pre-view



Lecture 2

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"Experiment meets theory"

- Collecting experimental data <u>physics/0311105</u>
 From detectors, over triggers to collision data at the LHC
- 2 Selection of dedicated signals
 Hypothesis testing, efficiency versus purity, use of Monte Carlo simulation, optimal event selection, significance
- ③ Performing measurements

Concepts of parameter estimation, counting experiments versus fitting distributions, least-square and maximum likelihood method, Neyman confidence belts (extension to Feldman-Cousins method)

④ Claiming discovery or setting limits
 Systematic uncertainties and significance, the CLs method













The Trigger: general layout



Signal selection



CERN LHC 10⁹ σ_{tot} E710 UA4/5 $\sigma_{b\,b}$ 10⁷ CDF UA1 = 10³⁴ cm⁻² sec⁻ 10⁵ 10³ θĥ Events / sec for CDF (pp) 10 UA1/2 $(p \bar{p})$ CDF/DO 10⁻¹ m_{top} = 174 GeV 10⁻³ 1.0 10 100

Fermilab SSC

Hypothesis testing



 $\begin{bmatrix} \text{``Error of type-1'': rejecting a signal event} \\ \text{``Error of type-2'': accepting a background event} \\ \text{or} \\ \begin{bmatrix} \epsilon_{\text{signal}} = \text{signal efficiency} = \# \text{Sel}_{\text{sign}} / \text{total } \# \text{ signal events} \\ \epsilon_{\text{bck}} = \text{background efficiency} = \# \text{Sel}_{\text{bck}} / \text{total } \# \text{ background events} \end{bmatrix}$

Hypothesis testing



Significance

The significance is influenced by systematic uncertainties

$$g(x'|\vec{\alpha}, \vec{\theta}) = \int R(x, x'|\vec{\alpha}) f_X(x|\vec{\theta}) dx$$

used to obtain the simulated distributions of variable x'

The imprecision of the model of R and f_X has to be taken into account when you estimate the background (and signal) rate after the event selection cuts \rightarrow for example an effect of $\Delta_{syst}B$

The significance is the amount of "standard deviations" the signal excess (=S) is above the background level (=B).

$$Sign = \frac{S}{\sqrt{Var[B]}} = \frac{S}{\sqrt{B}} \longrightarrow \frac{S}{\sqrt{Var_{stat}[B] + Var_{syst}[B]}} = \frac{S}{\sqrt{B + (\Delta_{syst}B)^2}}$$
Poisson distribution remember: $Var[X] = \sigma_X^2$

Significance



Significance



Multi-Variate Analysis \rightarrow combine variables \vec{x} into a single variable (optimal variable is the Likelihood Ratio variable from the optimal Neyman-Pearson hypothesis test)



(1) functional form $f_i(x_i)$ not known because from ∞ events use Monte Carlo simulation to approximate this

Multi-Variate Analysis \rightarrow combine variables \vec{x} into a single variable (optimal variable is the Likelihood Ratio variable from the optimal Neyman-Pearson hypothesis test)



2 histograms $h_i(x_i)$ from finite amount of events (normalized & use lots of simulation to get a fine binning)

Multi-Variate Analysis \rightarrow combine variables \vec{x} into a single variable (optimal variable is the Likelihood Ratio variable from the optimal Neyman-Pearson hypothesis test) $bin \ j \quad \to \quad \mathcal{LR}_i(x_{i,j}) = \frac{h_i^S(x_{i,j})}{h_i^S(x_{i,j}) + h_i^B(x_{i,j})}$ fit $\longrightarrow \mathcal{LR}_i(x_i)$ LR=1|R=1LR=1 $LR(x_1)$ -R(x₂) X_2 X_3 X_1 use histograms to calculate bin-per-bin a Likelihood Ratio (3)

④ fit these tendencies with an adequate function $\mathcal{LR}_i(x_i)$

Multi-Variate Analysis \rightarrow combine variables \vec{x} into a single variable



(5) combined into one variable per event $\mathcal{LR}(\vec{x})$ most optimal variable if the variables x_i are not correlated

Multi-Variate Analysis \rightarrow combine variables \vec{x} into a single variable



when linearly correlated, first rotate the variable space the set of new variables $\vec{X'} = \tilde{R} \cdot \vec{X}$ can be used into a LR method

(other MVA methods: Neural Networks, Boosted Decision Trees, Fisher Discriminant, ... MVA in ROOT: <u>http://tmva.sourceforge.net/</u>)

Now we have the selected data



Parameter estimation: the basics



Parameter estimation: the basics

The estimator of θ is function of the measurements $\{x'\}: \hat{\theta} = F(\{x'\})$ It is a stochastic variable which follows a distribution : $G(\hat{\theta})$



The distribution $G(\hat{\theta})$ depends on the value of the physics parameter θ itself.

The uncertainty on the estimator is related to the variance of the distribution $G(\hat{\theta})$.

But how to quote an uncertainty on the physical parameter θ itself?

Confidence belts (Neyman's method)



For each θ_0 , determine the distribution $G(\hat{\theta}|\theta_0)$.

Take the central $1-\alpha$ percent probability.

Defines $x_1(\theta_0)$ and $x_2(\theta_0)$.

These can be transformed into $\theta_1(x,\alpha)$ and $\theta_2(x,\alpha)$.

Now the data value x_{data} provides the 1- α confidence interval for the true value of θ , namely $[\theta_2, \theta_1]$.

$$1 - \alpha = P(\theta_2(x_{data}, \alpha) < \theta_{true} < \theta_1(x_{data}, \alpha))$$

1- α interval



Confidence belts (Neyman's method)



Feldman-Cousins

What to do when your measurement hints for a "non-physical" signal (eg. Branching Ratio above unity): Feldman-Cousins


Feldman-Cousins



where R_{input}^{best} is the most probable value of R_{input} for a given R (automatic switching between central and one-sided confidence regions)

Which estimator ?

 $1 - \alpha = P(R_2(R_{data}, \alpha) < R_{true} < R_1(R_{data}, \alpha))$



Counting experiments



Fitting distributions

$$g(x'|\vec{\alpha}, \vec{\theta}) = \int R(x, x'|\vec{\alpha}) f_X(x|\vec{\theta}) dx$$

If the information on the physics parameter θ of interest is hidden in a distribution g(x') rather than in an event rate, then we need to compare the expected distribution with the observed one.



Least-square method



Maximum Likelihood method

 $g(x'|\vec{\alpha},\vec{\theta}) = \int R(x,x'|\vec{\alpha}) f_X(x|\vec{\theta}) dx$

Calculate for each event a likelihood $g(x'|\vec{\alpha}, \vec{\theta}, m_t) \longrightarrow \mathcal{L}(m_t | x', \vec{\alpha}, \vec{\theta})$ Put them together $\mathcal{L}(m_t | \vec{x}, \vec{\alpha}, \vec{\theta}) = \prod_{i=1}^N \mathcal{L}(m_t | x'_i, \vec{\alpha}, \vec{\theta})$



Systematic uncertainties

$$g(x'|\vec{\alpha}, \vec{\theta}) = \int R(x, x'|\vec{\alpha}) f_X(x|\vec{\theta}) dx$$

There are uncertainties in the physics description f_X as well as in the experimental modelling R. Be clever, for the dominant systematic uncertainties try to fit the nuisance parameter α together with the physics parameter θ of interest.

This results in a reduced total uncertainty on the physics parameter of interest.

Example: top mass measurement and the jet energy scale



Confronting data with theory

Is my fancy model of new physics predicting a new particle present in the collision data or not ? *Monte Carlo simulation* theory



not ? Monte Carlo
simulation theory

$$g(x'|\vec{\alpha}, \vec{\theta}) = \int R(x, x'|\vec{\alpha}) f_X(x|\vec{\theta}) dx$$
experiment

$$g(m'_{4l}|\vec{\alpha}, \vec{\theta}, m_H) =$$

$$\int R(m_{4l}, m'_{4l}|\vec{\alpha}) f_X(x|\vec{\theta}, m_H) dm_{4l}$$
For each value of m_H we need to
compare the model with data

$$(m'_{4l}|\vec{\alpha}, \vec{\theta}, m_H) \leftarrow \rightarrow \text{data} = \{m'_{4l,i}\}$$

p-values

Quantify the level of agreement between the model (=hypothesis H_0) and the data without an explicit alternative hypothesis.

Collect the data $\{x_i\}$ into one test statistics T (another stochastic variable), which has a distribution $g(t|H_0)$. If T is defined such that large values of t reflect a worse agreement with data, then the p-value is defined as:



$$p = \int_{t_{obs}}^{\infty} g(t|H_0) dt$$

The p-value takes values between 0 and 1, and reflects the probability that a new experiment (in the same conditions) would results in a worse agreement with the hypothesis H_0 , given the hypothesis H_0 is correct. $\frac{n_i - h_i(m_H, \vec{\alpha}, \vec{\theta})}{\sqrt{h_i(m_H, \vec{\alpha}, \vec{\theta})}} \right)$

Eg.:
$$t=\chi^2=\sum_{i=1}^{n_{bins}}$$

p-values (eg. $H \rightarrow 4I$)

 $g(m'_{4l} | \vec{\alpha}, \vec{\theta}, m_H) \leftarrow \rightarrow \text{data} = \{m'_{4l,i}\}$



The CL_s method

We have the freedom to choose a test statistics to calculate the pvalues from the data \vec{n} , an example is based on the likelihood ratio



$$\longrightarrow t = -2lnQ(\vec{n})$$

The distribution of t can be obtained using "b-only" simulation or using "s+b" simulation.

This is the optimal test statistics if one uses the value of CL_S to characterize the signal confidence.

 $CL_s = \frac{CL_{s+b}}{1 - CL_b}$

For each m_H a value of CL_s using the data \vec{n} is obtained.

Setting limits (Higgs search)



Claiming discovery (Higgs boson)

 $5\sigma = 1$ in 3,5 million



... for most other analyses however the result is a limit ...

Summary of part 2

Theory versus Experiment - Experimental Techniques in Particle Physics - Jorgen D'Hondt (Vrije Universiteit Brussel)

Summary of part 2

Experiment meets theory!

① Detectors make our life complicated... deal with it!

2 The event selection (incl trigger) is essential in physics analyses

③ Different methods to estimate parameters... learn the differences! $g(x'|\vec{\alpha}, \vec{\theta}, m_H) \leftarrow \rightarrow \text{data} = \{x'_i\}$

④ When confronting data with theory limits are set or discoveries claimed

5 Experimentalists have a hard (but fruitful) life...

Big summary...

How to test your theory? $g(x'|\vec{\alpha}, \vec{\theta}) = \int R(x, x'|\vec{\alpha}) f_X(x|\vec{\theta}) dx$

- Test it yourself on existing results (part 1 of these lectures)
- 2 Make it available to experimentalists to be included in their analyses

(part 2 of these lectures)